HelixMC Documentation

Release 0.9

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HelixMC is a software package for Monte-Carlo (MC) simulations of DNA/RNA helices using the base-pair level model. It provides a powerful tool to understand the flexibility of DNA/RNA helices through numerical simulations.

The base-pair level model, first developed by Olson and colleagues, bridges between the simple elastic rod model and the full-atom representation, providing a reasonably sophisticated and yet computationally tractable way to model long DNA/RNA helices up to thousands of base-pairs and to evaluate their mechanical properties. HelixMC has the utility of applying external stretching forces and torques to the helix, and measuring the helix extension and the rotation of the helix (known as the linking number) during the process. This properly emulate the setup of recent single-molecule tweezers experiments, making HelixMC a useful tool for direct simulations of these experiments.

HelixMC is coded in Python in an object-oriented fashion. Rate-limiting core computations are speeded up using Cython. Therefore HelixMC provides a framework that is easy to use and to extend, as well as being reasonably fast when it comes to large-scale computations.
This tutorial demonstrates how to install and run simple calculations with HelixMC, and briefly summarizes available examples and bp-step parameter database. For details on the classes and functions available, please see HelixMC Reference.

1.1 Install

Currently HelixMC has only been tested on Linux. It should run on other Unix-like system (e.g. Mac OS X). The following packages are also required by HelixMC. The versions we used are given in parenthesis.

- Python (2.7.3)
- Numpy (1.6.1)
- Matplotlib (1.1.0)
- A working C/C++ compiler. Here we used GCC (4.6.3)

The easiest way to setup the python environment is to use latest Enthought Python Distribution (http://www.enthought.com/).

The easiest way to install is to use pip install:

```bash
$ pip install helixmc
```

Alternatively, one can download the source code from the latest GitHub repository. Simply run:

```bash
$ git clone https://github.com/fcchou/HelixMC.git
```

Or you can go to https://github.com/fcchou/HelixMC/ and download the source code by clicking the “Download ZIP” button.

After this, you can install HelixMC using setup.py:

```bash
$ python setup.py build
$ sudo python setup.py install
```

Instead of installing using setup.py, you can just add your HelixMC folder into the system’s $PATH and $PYTHONPATH. In bash this can be done by adding the following lines to your ~/.bashrc:
export PATH=$PATH:<HelixMC Path>
export PYTHONPATH=$PYTHONPATH:<HelixMC Path>

Then build the Cython extension. Under the helixmc/ folder, run:

$ python _cython_build.py build_ext --inplace

Note that this requires you to have Cython installed. Otherwise you can choose to build the c source file, then you do not need Cython:

$ python _c_build.py build_ext --inplace

Now you should be all set. To test the install, simply run:

$ helixmc-run --help

This should output the help information for helixmc-run application.

1.2 Run HelixMC

The helixmc-run application wraps the classes and functions of HelixMC to allow simple MC job submissions from command line.

A detailed help for all options of helixmc-run can be obtained by running:

$ helixmc-run --help

Now we demonstrate a simple example for helixmc-run.

First, run the following command to kick out a MC run:

$ helixmc-run -params DNA_default.npz -n_bp 100 -n_step 10 -seq GCCG -force 5 -compute_fuller_link -out_frame test_run

Here, -params give the input database file that contains bp-step parameters curated from PDB (by default it searches the helixmc database folder if it does not find the input file). -n_bp is the total number of bp in the helix. -n_step is the number of MC steps. -seq gives the sequence of the nucleic acids (ATCG for DNA and AUCG for RNA). -force is the applied z-direction stretching force. -compute_fuller_link tells HelixMC to compute and store the linking number using Fuller’s approximation [R1]. -out_frame option will make HelixMC save the final frame to disk as test_run.npz in this case.

Depending on your machine it will take a few seconds to run. After completion you should see something like:

Total time = 1.941772
Accept rate = 0.787879

It is advisable to check the Accept rate of each run, and make sure it is not too low. As a rule of thumb, if Accept rate < 0.1, this means most MC moves are rejected, and you will need use a higher-than-normal number of MC steps to achieve the same level of sampling.

Now we can analyze the output data. Open a Python session and enters the following:

>>> import numpy as np
>>> from helixmc.pose import HelixPose

The observables for each frame are stored in MC_data.npz. Normally the coordinates and reference frames of the last bp are recorded. If -compute_fuller_link or -compute_exact_link is used, the twist and writhe of the helix will also be stored (note that link = twist + writhe).
For example I can compute the average z-extension and the average link as follows:

```python
>>> data = np.load('MC_data.npz')
>>> data.files
['coord_terminal', 'twist', 'writhe', 'frame_terminal']
```

```python
>>> data['coord_terminal'][:,2] # 2 for the z-elements
array([ 309.06198311, 317.92717085, 320.17158221, 304.42561971,
        319.07461907, 306.94162915, 314.7566295 , 319.04106375,
        322.42125203, 325.72718993])
```

```python
>>> np.average(data['coord_terminal'][:,2]) # avg. z-extension in Å
315.95487393228649
```

```python
>>> np.average(data['twist'] + data['writhe']) # avg. link in radian
60.648749666780688
```

Remember we stored the final frame of the simulation to test_run.npz. We will now plot the helix using that:

```python
>>> pose = HelixPose('test_run.npz')
>>> pose.plot_centerline() # plot the centerline
>>> pose.plot_helix() # plot the entire helix
```

You should see something similar to the following

![Graphs showing z-extension and link](image)

This is the end of the example. For more examples, check the examples/ folder in HelixMC, which is briefly summarized below.

## 1.3 Other Examples

Here is a list of examples in the examples/ folder.

- **force_ext** This is just the example above.
- **link_cst** This is for link-constrained simulation, similar to the torsional-trap single-molecule experiment [R2].
- **z-dna** Simulation of Z-DNA using helixmc-run.
- **fuller_check** Check if the Fuller's approximation is correct in certain criteria.
- **data_fitting** How to use helixmc.fitfxn to fit simulation or experiment data to simple analytical models.
- **helixplot** More examples for plotting the helices.
How to perform alternative evaluation of bending persistence length using the method suggested by Olson et al. [R3].

bp_database  Examples on curating bp-step parameters from PDB.

## 1.4 Base-pair Step Parameters Database

In the helixmc/data/ folder, several different bp-step parameter sets are given. These datasets were all extracted from structures in Protein Data Bank (PDB, http://www.pdb.org/), with different selection and filtering. The list below summarizes these data.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>DNA_default</td>
<td>B-DNA data from structures with resolution (Rs) &lt;= 2.8 Å, excluding protein-binding models.</td>
</tr>
<tr>
<td>DNA_2.8_all</td>
<td>A-DNA + B-DNA, Rs &lt;= 2.8 Å, including protein-binding models.</td>
</tr>
<tr>
<td>DNA_2.0_noprot</td>
<td>B-DNA, Rs &lt;= 2.0 Å, excluding protein-binding models.</td>
</tr>
<tr>
<td>RNA_default</td>
<td>RNA, Rs &lt;= 2.8 Å, excluding protein-binding models.</td>
</tr>
<tr>
<td>RNA_2.8_all</td>
<td>RNA, Rs &lt;= 2.8 Å, including protein-binding models.</td>
</tr>
<tr>
<td>RNA_2.0_noprot</td>
<td>RNA, Rs &lt;= 2.0 Å, excluding protein-binding models.</td>
</tr>
<tr>
<td>Z-DNA</td>
<td>Z-DNA, Rs &lt;= 2.8 Å, including protein-binding models.</td>
</tr>
<tr>
<td>*unfiltered</td>
<td>Unfiltered datasets (no filtering of histogram outliers).</td>
</tr>
<tr>
<td>DNA_gau</td>
<td>Single 6D Gaussian built from DNA_default.</td>
</tr>
<tr>
<td>RNA_gau</td>
<td>Single 6D Gaussian built from RNA_default.</td>
</tr>
<tr>
<td>DNA_gau_graft</td>
<td>Chimera dataset with mean from DNA_gau and covariance from RNA_gau.</td>
</tr>
<tr>
<td>RNA_gau_graft</td>
<td>Chimera dataset with mean from RNA_gau and covariance from DNA_gau.</td>
</tr>
<tr>
<td>*gau_refit</td>
<td>Manually refitted datasets to match experimental measurements.</td>
</tr>
<tr>
<td>*2.8_all?bp</td>
<td>Multi-bp datasets derived from the 2.8_all pdb lists.</td>
</tr>
</tbody>
</table>

Note that Gaussian dataset (*gau*.npy) must be loaded with -gaussian_params tag in helixmc-run command line (instead of -params). Also Gaussian dataset does not support sequence specific simulations.

The corresponding lists of PDB models being used are given in the helixmc/data/pdb_list/ folder.

These datasets are in npy/npz format (Numpy array/archive). For the npz files, the data for different bp-steps of different sequences were separated into different arrays in the file. For B-DNA and RNA, parameter sets with Rise >= 5.5 Å or Twist <= 5° were thrown away as outliers. Then, parameter sets with values beyond 4 standard deviations away from the mean for any of the 6 bp-step parameters were also removed. For B-DNA (except DNA_2.8_all, where the protein binding makes A-DNA and B-DNA unseparable), we further clustered the data using k-means algorithm to separate the A-DNA and B-DNA data. Note that these filtering steps are skipped in the unfiltered datasets.

For Z-DNA, we only considered two types of bp-steps: CG and GC. We used the following selection criteria: Twist <= -30° for GC, and -30° < Twist <= 5° for CG. For CG bp-steps, we further filtered the data by only keeping parameter sets with 4.5 Å <= Rise < 6.3 Å. Parameter sets with values beyond 4 standard deviation away from the mean were then removed, similar to the above cases.

See also examples/bp_database/ for a detailed example for the curation of DNA_2.0_noprot.npz.

## 1.5 References
This reference document details functions, modules, and objects included in HelixMC, describing what they are and what they do. For learning how to use HelixMC, see also HelixMC Tutorial.

### 2.1 Code Organization

HelixMC is coded in Python in an object-oriented fashion, allowing easy usage and extension. Here we briefly summarize the organization of the code.

First, `HelixPose` object stores all information of the current helix conformation. Various properties, e.g. coordinates, twist, writhe, etc. can be directly accessed from the object. The object also contains functions that allow one to update the conformation and to plot the helix.

Second, `RandomStep` are used to generate random samples of base-pair step parameters. `RandomStepSimple` takes in a list of database parameter sets, and can randomly emit one of input parameter set, or construct a multivariate Gaussian and emit samples from the distribution, upon the choice of the user. `RandomStepAgg` aggregates multiple `RandomStep` objects into one, allow easy handling of sequence-dependent sampling (by aggregating several `RandomStepSimple` for different sequences). The user can also create their own `RandomStep` objects by inheriting from `RandomStepBase`.

Third, `Score` objects take a `HelixPose` and scores it. The scoring can then be used to decide whether a Monte-Carlo move should be accepted. Currently we have 3 simple score terms `ScoreExt`, `ScoreTorsionTrap` and `ScoreXyTrap`, which scores a HelixPose under Z-extension, torsional trap and xy horizontal trap respectively. These 3 score terms are summarized into `ScoreTweezers`, which is a sub-class of `ScoreAgg`, an aggregator class that combines multiple score functions. `ScoreTweezers` is the workhorse score functions currently in used. The user can also define their own scoring by inheriting from `ScoreBase`.

Last, the `util` module contains useful functions for evaluating twist and writhe, for conversion between bp-step parameters and cartesian translation and rotation operation, and so on. The `fitfxn` module is a standalone module that contains a few widely used analytical fitting functions based on the elastic rod model.

### 2.2 Constant Random Seed

```python
constant_seed([seed])  # Set constant random seed.
```
2.2.1 helixmc.constant_seed

helixmc.constant_seed(seed=24601)

Set constant random seed.

**Parameters**

- **seed**: int, optional
  Random seed.

2.3 Helix Pose

pose.HelixPose(params[, frame0, compute_tw_wr]) Pose object storing the state info of the helix.

2.3.1 helixmc.pose.HelixPose

class helixmc.pose.HelixPose (params, frame0=None, compute_tw_wr=False)

Pose object storing the state info of the helix.

**Parameters**

- **params**: ndarray of (N,6)
  List of all bp-step parameters. A N bp helix has (N-1)*6 parameters.

- **frame0**: ndarray of (3,3), optional
  The frame of the first base-pair, default is np.eye(3) (overlaps with global coordinate).

- **compute_tw_wr**: bool, optional
  Whether to compute twist and writhe (Fuller writhe) during system update. Should be set to True for link-constrained simulations.

**Attributes**

<table>
<thead>
<tr>
<th>attribute</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td>compute_tw_wr</td>
<td>(bool) See Parameters section above.</td>
</tr>
<tr>
<td>writhe_exact</td>
<td>(float) Exact writhe of the helix.</td>
</tr>
<tr>
<td>writhe_fuller</td>
<td>(float) Fuller’s writhe of the helix.</td>
</tr>
<tr>
<td>twist</td>
<td>(float) Supercoiling twist of the helix.</td>
</tr>
<tr>
<td>coord_terminal</td>
<td>(1d array of (3)) Coordinate (x,y,z) of the center of last base-pair.</td>
</tr>
<tr>
<td>frame_terminal</td>
<td>(ndarray of (3,3)) Coordinate frame of the last base-pair. Each column represent the corresponding axis (frame[:,0] is the x-axis etc.)</td>
</tr>
<tr>
<td>z_terminal</td>
<td>(float) Z-component of coord_terminal</td>
</tr>
<tr>
<td>link_fuller</td>
<td>(float) Link of the helix computed using Fuller’s approximation.</td>
</tr>
<tr>
<td>link_exact</td>
<td>(float) Exact link of the helix.</td>
</tr>
<tr>
<td>n_bp</td>
<td>(int) Number of base-pairs in the helix.</td>
</tr>
<tr>
<td>coord</td>
<td>(ndarray of (N,3)) Coordinates of all base-pairs in the helix (n_bp entries).</td>
</tr>
<tr>
<td>dr</td>
<td>(ndarray of (N,3)) Delta-r vectors of the entire helix (n_bp-1 entries).</td>
</tr>
<tr>
<td>frames</td>
<td>(ndarray of (N,3,3)) Frames of all base-pairs in the helix (n_bp entries).</td>
</tr>
<tr>
<td>params</td>
<td>(ndarray of (N,6)) List of all bp-step parameters in the helix (n_bp-1 entries).</td>
</tr>
<tr>
<td>rb_vec</td>
<td>(ndarray of (N,3)) Ribbon vectors of all base-pairs in the helix (n_bp entries).</td>
</tr>
</tbody>
</table>

**__init__** (params, frame0=None, compute_tw_wr=False)
accept_update()  
Accept a trial update.

copy()  
Return a copy of the current pose.

    Returns pose_copy : HelixPose  
    Copy of the current pose.

classmethod from_file(input_file, compute_tw_wr=False)  
Load pose data from an input file.

    Parameters input_file : str  
        Input file (.npz) that stores the helix pose data.
    
        compute_tw_wr : bool, optional  
        Whether to compute twist and writhe (Fuller writhe) during system update. Should be set to True for link-constrained simulations.
    
    Raises ValueError  
        If n_bp < 2 in the input file.

guess_twist_center()  
Attempt to guess the twist center value. Use circmean of the current twists.

plot_centerline(color='k', show=True, fig_ax=None)  
Plot the helix center-line using matplotlib + mplot3d.

    Parameters color : str, optional  
        Colors of the centerline (matplotlib color codes).
    
        show : bool, optional  
        Whether to invoke pyplot.show() method at the end.
    
        fig_ax : mplot3d.Axes3D, optional  
        Input mplot3d.Axes3D object. For plotting multiple helix on the same graph.

plot_helix(rb_width=5.0, color='kb', show=True, fig_ax=None)  
Plot the helix using matplotlib + mplot3d.

    Parameters rb_width : float, optional  
        Width of the helix ribbon in Å.
    
        color : str, optional  
        Colors of the plot (matplotlib color codes), first letter for backbond and second letter for base-pair.
    
        show : bool, optional  
        Whether to invoke pyplot.show() method at the end.
    
        fig_ax : mplot3d.Axes3D, optional  
        Input mplot3d.Axes3D object. For plotting multiple helix on the same graph.

reject_update()  
Reject a trial update.
set_params \((\text{params}, \text{frame0}=\text{None})\)

Set the bp-step params of the HelixPose.

**Parameters**  
- **params**: ndarray of (N,6), optional
  
  List of all bp-step parameters. Number of params should equal to \(n_{\text{bp}} - 1\).

- **frame0**: ndarray of (3,3)
  
  The frame of the first base-pair, default is \(\text{np.eye}(3)\).

update \((i, \text{params}, o=\text{None}, R=\text{None})\)

Full update of the \(i\)-th bp-step.

**Parameters**  
- **i**: int
  
  The index of the bp-step to be updated.

- **params**: ndarray
  
  Input base-pair step parameter set.

- **o**: ndarray, optional
  
  Coordinates for the bp-centers of the 2nd base-pair.

- **R**: ndarray, optional
  
  Rotational matrix for the transformation.

Raises **ValueError**  

If \(i < 0\) or \(i >= n_{\text{bp}}\).

update_trial \((i, \text{params}, o=\text{None}, R=\text{None})\)

Trial update of the \(i\)-th bp-step. Following accept_update or reject_update is required.

**Parameters**  
- **i**: int
  
  The index of the bp-step to be updated.

- **params**: ndarray
  
  Input base-pair step parameter set.

- **o**: ndarray, optional
  
  Coordinates for the bp-centers of the 2nd base-pair.

- **R**: ndarray, optional
  
  Rotational matrix for the transformation.

Raises **ValueError**  

If \(i < 0\) or \(i >= n_{\text{bp}}\).

write2disk \((\text{filename})\)

Write the current pose to disk.

**Parameters**  
- **filename**: str
  
  Name of the output file.

### 2.4 Random Base-pair Steps Generators
2.4.1 helixmc.random_step.RandomStepBase

class helixmc.random_step.RandomStepBase
    Base class for Random bp-step generator, for inheritance only.

    See also:

    RandomStepSimple  Simple random bp-step generator.

    RandomStepAgg    Random bp-step generator by aggregating multiple independent bp-step generators.

__call__

__init__

2.4.2 helixmc.random_step.RandomStepSimple

class helixmc.random_step.RandomStepSimple
    Simple random bp-step generator. Pick random datasets from database or sample from a multivariate Gaussian
    built from the database.

    Parameters
    ----------
    params : ndarray, shape (N,6), optional
        Input base-pair step parameters. Usually obtained by analyzing the structures in PDB. Must be specified if
        params_cov and params_avg is not being input, or if gaussian_sampling is set to False. Order = [Shift, Slide, Rise, Tilt, Roll, Twist] Distance in
        unit of Å, angle in unit of radians.

    params_cov : ndarray, shape (6,6), optional
        Covariance matrix of the multivariate Gaussian for step parameters. Used for Gaussian sampling.

    params_avg : ndarray, shape (6,6), optional
        Averages of the multivariate Gaussian for step parameters. Used for Gaussian sampling.

    gaussian_sampling : bool, optional
        Whether to sample assuming a multivariate Gaussian. Default is True.

    Raises
    -----
    ValueError
        If params is not specified, and either params_avg and params_cov are not specified. If
        params is not specified, but gaussian_sampling is set to False.

    See also:

    RandomStepBase  Base class for Random bp-step generator, for inheritance only.

    RandomStepAgg    Random bp-step generator by aggregating multiple independent bp-step generators.
Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>gaussian_sampling</td>
<td>(bool) See the Parameters section.</td>
</tr>
<tr>
<td>params_avg</td>
<td>(ndarray) See the Parameters section.</td>
</tr>
<tr>
<td>params_cov</td>
<td>(ndarray) See the Parameters section. Return None if not specified at init.</td>
</tr>
<tr>
<td>params</td>
<td>(ndarray) See the Parameters section. Return None if not specified at init.</td>
</tr>
</tbody>
</table>

___call__()

Draw one random bp-step parameter set from the distribution.

**Returns**

- params: ndarray, shape (6)
  Randomly generated bp-step parameter set.
- o: ndarray, shape (3)
  Corresponding bp-center for the 2nd bp of the bp-step (1st bp is at origin and oriented with the coordinate frame).
- R: ndarray, shape (3,3)
  Corresponding frame for the 2nd bp of the bp-step.

___init__ (params=None, params_cov=None, params_avg=None, gaussian_sampling=True)

__classmethod__ load_gaussian_params (filename)

Load a single Gaussian parameter file from disk.

**Parameters**

- filename: str
  Name of the Gaussian parameter file, in .npy or plain text format. First row is the mean parameters and the following six rows represents the covariance matrix. The routine will look for helixmc/data/ if the file is not found in current folder. Order = [Shift, Slide, Rise, Tilt, Roll, Twist] Distance in unit of Å, angle in unit of radians.

**Returns**

- random_step: RandomStepSimple
  Random step generator corresponds to the input file.

__classmethod__ load_params (filename, gaussian_sampling=True)

Load a simple bp-step parameter file from disk.

**Parameters**

- filename: str
  Name of the parameter file, in .npy or text format. It should be a (N * 6) numpy array. Each row contains the 6 step parameters. The routine will look for helixmc/data/ if the file is not found in current folder. Order = [Shift, Slide, Rise, Tilt, Roll, Twist] Distance in unit of Å, angle in unit of radians.

- gaussian_sampling: bool, optional
  Whether to sample assuming a multivariate Gaussian.

**Returns**

- random_step: RandomStepSimple
  Random step generator corresponds to the input file.

2.4.3 helixmc.random_step.RandomStepAgg

__class__ helixmc.random_step.RandomStepAgg (data_file=None, gaussian_sampling=True)

Random bp-step generator by aggregating multiple independent simple bp-step generators. Useful for sequence dependence simulations.
**Parameters**

- **data_file** : str, optional
  
  Pre-curated database file with sequence dependence in .npz format.

- **gaussian_sampling** : bool, optional
  
  Whether to sample assuming a multivariate Gaussian. Default is True.

**See also:**

- **RandomStepBase** Base class for Random bp-step generator, for inheritance only.
- **RandomStepSimple** Simple random bp-step generator.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>gaussian_sampling</strong></td>
<td>(bool) See the Parameters section.</td>
</tr>
<tr>
<td><strong>params_avg</strong></td>
<td>(ndarray) Average values for the step parameters distribution.</td>
</tr>
<tr>
<td><strong>rand_list</strong></td>
<td>(list) List of all RandomStep objects in the aggregation.</td>
</tr>
<tr>
<td><strong>names</strong></td>
<td>(list) List of all names of RandomStep in the aggregation.</td>
</tr>
</tbody>
</table>

**__call__**(identifier=None)

Draw one random bp-step parameter set from the distribution. Randomly select one generator in the aggregation and return its generated result if no input parameter is given.

**Parameters**

- **identifier** : int or str
  
  Index or name of the requested random step generator.

**Returns**

- **params** : ndarray, shape (6)
  
  Randomly generated bp-step parameter set.

- **o** : ndarray, shape (3)
  
  Corresponding bp-center for the 2nd bp of the bp-step (1st bp is at origin and oriented with the coordinate frame).

- **R** : ndarray, shape (3,3)
  
  Corresponding frame for the 2nd bp of the bp-step.

**Raises** **TypeError**:

- If the input identifier is not int or str

**__init__**(data_file=None, gaussian_sampling=True)

**append_random_step**(name, random_step)

Append one additional random bp-step generator to the aggregation.

**Parameters**

- **name** : str
  
  Name of the random bp-step generator.

- **random_step** : subclass of RandomStepBase
  
  The random bp-step generator to be added to the aggregation.

**Raises** **TypeError**

- If random_step does not belong to a subclass of RandomStepBase.

**ValuError**

- If the input name already exists in self.names.

### 2.4. Random Base-pair Steps Generators


clear_all()
    Clear all random bp-step generator in the aggregation.

get_rand_step(identifier)
    Return one RandomStep object stored in the aggregation.
    
    Parameters identifier : int or str
        Index or name of the requested random step generator.
    
    Returns rand_step : subclass of RandomStepBase
        RandomStep object stored in the aggregation.
    
    Raises TypeError :
        If the input identifier is not int or str

load_from_file(data_file)
    Load data file in .npz format and append to the current aggregation. The routine will look for helixmc/data/ if the file is not found in current folder.
    
    Parameters data_file : str, optional
        Pre-curated database file with sequence dependence in .npz format.

name2rand_idx(name)
    Get the index of a RandomStep object in rand_list from its name.
    
    Parameters name : str
        Name of the RandomStep in the aggregation.
    
    Returns idx : int
        The corresponding index of the RandomStep object.

2.5 Score Functions

| score.ScoreBase() | Base class for scoring function, for inheritance only. |
| score.ScoreExt(force) | Score function for force-extension along Z-axis. |
| score.ScoreTorsionTrap(stiffness, target_link) | Score function for torsional trap. |
| score.ScoreXyTrap(stiffness) | Score function for xy trap. |
| score.ScoreAgg([score_list]) | Score function aggregates of multiple score terms. |
| score.ScoreTweezers([force, ...]) | Score function for tweezers experiments. |

2.5.1 helixmc.score.ScoreBase

class helixmc.score.ScoreBase
    Base class for scoring function, for inheritance only.
    
    __call__(pose)
    __init__()
2.5.2 helixmc.score.ScoreExt

class helixmc.score.ScoreExt (force)
Score function for force-extension along Z-axis.

Parameters
force : float
Applied z-direction force to the helix, in pN.

Attributes

__call__ (pose)
Score the input pose.

Parameters
pose : HelixPose
Input pose for scoring.

Returns
score : float
Score of the pose.

__init__ (force)

2.5.3 helixmc.score.ScoreTorsionTrap

class helixmc.score.ScoreTorsionTrap (stiffness, target_link)
Score function for torsional trap.

Parameters
stiffness : float
The stiffness of the torsional trap, in pN.Å.

target_link : float
Center of the harmonic torsional trap (link), in radians.

Attributes

stiffness : (float)

target_link : (float) See Parameters section above.

__call__ (pose)
Score the input pose.

Parameters
pose : HelixPose
Input pose for scoring.

Returns
score : float
Score of the pose.

__init__ (stiffness, target_link)
2.5.4 helixmc.score.ScoreXyTrap

class helixmc.score.ScoreXyTrap (stiffness)
Score function for xy trap.

Parameters stiffness: float
The stiffness of the xy trap, in pN/Å.

Attributes

<table>
<thead>
<tr>
<th>stiffness</th>
<th>(float) See Parameters section above.</th>
</tr>
</thead>
</table>

__call__ (pose)
Score the input pose.

Parameters pose: HelixPose
Input pose for scoring.

Returns score: float
Score of the pose.

__init__ (stiffness)

2.5.5 helixmc.score.ScoreAgg

class helixmc.score.ScoreAgg (score_list=[])
Score function aggregates of multiple score terms.

Parameters score_list: list, optional
List of score terms (subclass of ScoreBase) in this score.

Attributes

<table>
<thead>
<tr>
<th>score_list</th>
<th>(list) See Parameters section above.</th>
</tr>
</thead>
<tbody>
<tr>
<td>is_empty</td>
<td>(bool) If the score_list is empty.</td>
</tr>
</tbody>
</table>

__call__ (pose)
Score the input pose.

Parameters pose: HelixPose
Input pose for scoring.

Returns score: float
Score of the pose.

__init__ (score_list=[])

append (score_term)
Append new score term.

Parameters score_term: subclass of ScoreBase
Score term to be appended.
clear()
Clear the score_list.

2.5.6 helixmc.score.ScoreTweezers

class helixmc.score.ScoreTweezers (force=0, torsional_stiffness=0, target_link=None, xy_stiffness=0)
Score function for tweezers experiments.

Parameters

force : float, optional
Applied z-stretching force, in pN.

torsional_stiffness : float, optional
Stiffness of the torsional trap, in pN.Å.

target_link : float, optional
Center of the torsional trap (link), in radians.

xy_stiffness : float, optional
Stiffness of xy trap, in pN.Å.

__init__ (force=0, torsional_stiffness=0, target_link=None, xy_stiffness=0)

2.6 Utility Functions

2.6.1 Rotation Matrices

util.Rz(theta)  \hspace{1cm} \text{Return } z\text{-rotation matrices with rotational angle theta.}
util.Rx(theta)  \hspace{1cm} \text{Return } x\text{-rotation matrices with rotational angle theta.}
util.Ry(theta)  \hspace{1cm} \text{Return } y\text{-rotation matrices with rotational angle theta.}
util.R_axis(theta, axis) \hspace{1cm} \text{Return rotation matrices with rotational angle theta along an arbitrary rotation axis.}

helixmc.util.Rz

helixmc.util.Rz (theta)
Return z-rotation matrices with rotational angle theta.

Parameters

theta : array-like
Rotation angles of the matrix in radians.

Returns

rot_matrix : ndarray
Corresponding z-rotation matrices for each input angle, align with the first index.

See also:

Ry  \hspace{1cm} \text{Return } y\text{-rotation matrices with rotational angle theta.}
Rx  \hspace{1cm} \text{Return } x\text{-rotation matrices with rotational angle theta.}
R_axis  \hspace{1cm} \text{Return rotation matrices with rotational angle theta along an arbitrary rotation axis.}
helixmc.util.Rx

helixmc.util.Rx\( (\theta) \)
Return x-rotation matrices with rotational angle \( \theta \).

Please refer to the documentation for \( R_z \) for further details.

See also:
\( R_z, R_y, R_axis \)

helixmc.util.Ry

helixmc.util.Ry\( (\theta) \)
Return y-rotation matrices with rotational angle \( \theta \).

Please refer to the documentation for \( R_z \) for further details.

See also:
\( R_z, R_x, R_axis \)

helixmc.util.R_axis

helixmc.util.R_axis\( (\theta, axis) \)
Return rotation matrices with rotational angle \( \theta \) along an arbitrary rotation axis.

Parameters \( \theta \) : array-like
Rotation angles of the matrix in radians.

\( axis \) : ndarray, shape (N,3)
Rotational axis for the rotation being performed, align with first index (i.e. axis[3] is the rotational axis for angle \( \theta[3] \)).

Returns \( rot_matrix \) : ndarray
Corresponding rotation matrices for each input angle, align with the first index.

See also:
\( R_z \) Return z-rotation matrices with rotational angle \( \theta \).
\( R_y \) Return y-rotation matrices with rotational angle \( \theta \).
\( R_x \) Return x-rotation matrices with rotational angle \( \theta \).

2.6.2 Twist and Writhe

util.ribbon_twist\( (dr, rb_vec[, ...]) \)
Compute the ribbon-twist (supercoiling twist) of a helix.

util.writhe_exact\( (dr) \)
Compute the writhe of the helix using the exact Gauss double integral.

util.writhe_Fuller\( (dr[, return_val_only]) \)
Compute the writhe using the Fuller’s approximated single integral.

helixmc.util.ribbon_twist

helixmc.util.ribbon_twist\( (dr, rb_vec, return_val_only=True, twist_center=0.0) \)
Compute the ribbon-twist (supercoiling twist) of a helix.
Parameters `dr` : ndarray, shape (N,3)
    Input delta_r vectors (dr[i] = r[i+1] - r[i]).

`rb_vec` : ndarray, shape (N+1,3)
    The ribbon vectors for the helix, equals to `frame[:,:,1]` in the current setting. Must
    be normalized vectors.

`return_val_only` : bool, optional
    If True, return one float value for the overall twist of the system. Otherwise return the
    individual twists for each bp-step. Default set to True.

`twist_center` : float, optional
    Fold the step twists to (center - pi, center + pi], default to 0.

Returns `twist` : float or ndarray of shape (N)
    The overall twist or the individual twists of the helix. See the `return_val_only` parameter above.

Raises `ValueError`
    If dr.shape[0] != rb_vec.shape[0] + 1.

See also:

`writhe_fuller` Compute the writhe of the helix using the Fuller approximated single integral.

`writhe_exact` Compute the writhe of the helix using the exact Gauss double integral.

`helixmc.util.writhe_exact`

`helixmc.util.writhe_exact(dr)`
    Compute the writhe of the helix using the exact Gauss double integral. O(N^2) complexity.

Parameters `dr` : ndarray, shape (N,3)
    Input delta_r vectors (dr[i] = r[i+1] - r[i]).

Returns `writte` : float
    The overall writhe of the helix.

See also:

`writhe_fuller` Compute the writhe of the helix using the Fuller approximated single integral.

`ribbon_twist` Compute the ribbon-twist of a helix.

Notes

Details of the evaluation scheme is dicussed in reference 1 2.

References

**helixmc.util.writhe_fuller**

**helixmc.util.writhe_fuller** *(dr, return_val_only=True)*

Compute the writhe using the Fuller’s approximated single integral. Only guarantee to be correct modulo 4 pi. O(N) complexity.

**Parameters**

- **dr**: ndarray, shape = (N,3)
  
  Input delta_r vectors (dr[i] = r[i+1] - r[i]).

- **return_val_only**: bool, optional
  
  If True, return one float value for the overall writhe of the system. Otherwise return the individual writhe contribution for each bp-step. Default set to True.

**Returns**

- **writhe**: float or ndarray of shape(N)
  
  The overall writhe of the helix or the individual writhe contribution for each bp-step. See the ‘return_val_only’ parameter above.

**See also:**

- **writhe_exact** Compute the writhe of the helix using the exact Gauss double integral.
- **ribbon_twist** Compute the ribbon-twist of a helix.

**Notes**

See **writhe_exact** for references on details of the evaluation scheme.

### 2.6.3 Useful Conversions

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>util.params2coords</strong> (params)</td>
<td>Convert base-pair step parameters to bp-center coordinates and rotation matrix.</td>
</tr>
<tr>
<td><strong>util.coords2params</strong> (o2, R2)</td>
<td>Convert bp-center coordinates and rotation matrix to base-pair step parameters.</td>
</tr>
<tr>
<td><strong>util.dr2coords</strong> (dr)</td>
<td>Convert delta_r vectors to coordinates.</td>
</tr>
<tr>
<td><strong>util.coords2dr</strong> (coord)</td>
<td>Convert xyz coordinates of axis curve to delta_r vectors.</td>
</tr>
<tr>
<td><strong>util.params2data</strong> (params[, frame0])</td>
<td>Convert step parameters to delta_r vectors and frames.</td>
</tr>
<tr>
<td><strong>util.data2params</strong> (dr, frames)</td>
<td>Convert delta_r vectors and frames to step parameters.</td>
</tr>
<tr>
<td><strong>util.params_join</strong> (params)</td>
<td>Convert consecutive bp-params to the params between 1st and last bp.</td>
</tr>
<tr>
<td><strong>util.frames2params</strong> (o1, o2, f1, f2)</td>
<td>Convert bp coordinates and frames to step parameters.</td>
</tr>
<tr>
<td><strong>util.frames2params_3dna</strong> (o1, o2, f1, f2)</td>
<td>Convert bp coordinates and frames in 3DNA format to step parameters.</td>
</tr>
</tbody>
</table>

**helixmc.util.params2coords**

**helixmc.util.params2coords** *(params)*

Convert base-pair step parameters to bp-center coordinates and rotation matrix.

**Parameters**

- **params**: ndarray, shape (N,6)
  
  Input base-pair step parameters. Distances in unit of Å, angles in unit of radians. Order = [Shift, Slide, Rise, Tilt, Roll, Twist]

**Returns**

- **o2**: ndarray, shape (N,3)
Coordinates for the bp-centers of the 2nd base-pair.

\( \textbf{R}_2 \) : ndarray, shape (N,3,3)
Rotational matrix for the transformation.

See also:

\texttt{coords2params}  Convert bp-center coordinates and rotation matrix to base-pair step parameters.

\texttt{helixmc.util.coords2params}

\texttt{helixmc.util.coords2params} (o2, R2)
Convert bp-center coordinates and rotation matrix to base-pair step parameters. The frame of bp1 is used as reference ( o1 = [0 0 0] and R1 = np.eye(3) )

Parameters o2 : ndarray, shape (N,3)
Coordinates for the bp-centers of the 2nd base-pair.

R2 : ndarray, shape (N,3,3)
Rotational matrix for the transformation.

Returns Base-pair step parameters.
Distance in unit of Å, angle in unit of radians. Order = [Shift, Slide, Rise, Tilt, Roll, Twist]

See also:

\texttt{params2coords}  Convert base-pair step parameters to bp-center coordinates and rotation matrix.

\texttt{helixmc.util.dr2coords}

\texttt{helixmc.util.dr2coords} (dr)
Convert delta-r vectors to coordinates.

Parameters dr : ndarray, shape (N,3)
Input delta_r vectors (dr[i] = r[i+1] - r[i]).

Returns coord : ndarray, shape (N+1,3)
Coordinates for the base-pair-centers (r[i]).

See also:

\texttt{coords2dr}  Convert xyz coordinates of axis curve to delta-r vectors.

\texttt{helixmc.util.coords2dr}

\texttt{helixmc.util.coords2dr} (coord)
Convert xyz coordinates of axis curve to delta-r vectors.

Parameters coord : ndarray, shape (N,3)
The axis curve xyz coordinates in unit of Å (r vectors).

Returns dr : ndarray, shape (N,3)

2.6. Utility Functions
Delta-r vectors \((\text{dr}[i] = \text{r}[i+1] - \text{r}[i])\).

See also:

**dr2coords** Convert delta-r vectors to coordinates.

**helixmc.util.params2data**

**helixmc.util.params2data** (*params*, *frame0=None*)

Convert step parameters to delta-r vectors and frames.

**Parameters**

- **params** : ndarray, shape (N,6)
  
  Input base-pair step parameters. Order = [Shift, Slide, Rise, Tilt, Roll, Twist] Distance in unit of Å, angle in unit of radians.

- **frame0** : ndarray, shape (3,3), optional
  
  The frame for the 1st base-pair. Default set to np.eye(3).

**Returns**

- **dr** : ndarray, shape (N,3)
  
  Delta-r vectors \((\text{dr}[i] = \text{r}[i+1] - \text{r}[i])\).

- **frames** : ndarray, shape (N+1,3,3)
  
  Frame of each base-pair.

See also:

**data2params** Convert delta-r vectors and frames to step parameters.

**helixmc.util.data2params**

**helixmc.util.data2params** (*dr*, *frames*)

Convert delta-r vectors and frames to step parameters.

**Parameters**

- **dr** : ndarray, shape (N,3)
  
  Delta-r vectors \((\text{dr}[i] = \text{r}[i+1] - \text{r}[i])\).

- **frames** : ndarray, shape (N+1,3,3)
  
  Frame of each base-pair.

**Returns**

- **params** : ndarray, shape (N,6)
  
  Base-pair step parameters. Distance in unit of Å, angle in unit of radians. Order = [Shift, Slide, Rise, Tilt, Roll, Twist]

See also:

**params2data** Convert step parameters to delta-r vectors and frames.

**helixmc.util.params_join**

**helixmc.util.params_join** (*params*)

Convert consecutive bp-params to the params between 1st and last bp.

**Parameters**

- **params** : ndarray, shape (N,6)
Input base-pair step parameters. Distances in unit of Å, angles in unit of radians. Order = [Shift, Slide, Rise, Tilt, Roll, Twist]

**Returns params** : ndarray, shape (6)
Base-pair step parameters between 1st and last.

```python
helixmc.util.frames2params
```

Convert bp coordinates and frames to step parameters.

**Parameters**

- `ol` : ndarray, shape (N,3)
  Origins for the bp-centers of the 1st base-pair.
- `o2` : ndarray, shape (N,3)
  Origins for the bp-centers of the 2nd base-pair.
- `f1` : ndarray, shape (N,3,3)
  Frames for the 1st base-pair.
- `f2` : ndarray, shape (N,3,3)
  Frames for the 2nd base-pair.

**Returns params** : ndarray, shape (N,6)
Base-pair step parameters. Distance in unit of Å, angle in unit of radians. Order = [Shift, Slide, Rise, Tilt, Roll, Twist]

See also:

- `frames2params_3dna` Convert bp coordinates and frames in 3DNA format to step parameters.

```python
helixmc.util.frames2params_3dna
```

Convert bp coordinates and frames in 3DNA format to step parameters. Note that the 3DNA base-pair frames differ from HelixMC by a transpose operation.

See also:

- `frames2params` Convert bp coordinates and frames to step parameters.

### 2.6.4 Other Functions

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>util.unitarize(R)</code></td>
<td>Enforce unitarity of the input matrix using Gram-Schmidt process.</td>
</tr>
<tr>
<td><code>util.circmean(arr[, axis])</code></td>
<td>Circular mean of angles.</td>
</tr>
<tr>
<td><code>util.MC_acpt_rej(score_old, score_new[, kT])</code></td>
<td>Decide whether to accept a Monte-Carlo move.</td>
</tr>
<tr>
<td><code>util.read_seq_from_fasta(fasta)</code></td>
<td>Read the sequence from a fasta file.</td>
</tr>
<tr>
<td><code>util.locate_data_file(data_file)</code></td>
<td>Search for the input data file.</td>
</tr>
</tbody>
</table>
**helixmc.util.unitarize**

helixmc.util.unitarize($R$)

Enforce unitarity of the input matrix using Gram-Schmidt process. This function modifies the input matrix inplace.

**Parameters**
- $R$ : ndarray, shape (N,3,3)
  (List of) input matrix to be unitarized.

**Returns**
- $R$ : ndarray, shape (N,3,3)
  Unitarized input matrix.

**helixmc.util.circmean**

helixmc.util.circmean(arr, axis=None)

Circular mean of angles. Results are in [-pi, pi]. Note that scipy.stats has a similar function, but we re-implement it because the scipy one depends on its version.

**Parameters**
- arr : ndarray
  Input numpy array.
- axis : int, optional
  Axis on which the mean is computed.

**Returns**
- mean : ndarray
  The circular mean.

**helixmc.util.MC_acpt_rej**

helixmc.util.MC_acpt_rej(score_old, score_new, kT=41.164043971999995)

Decide whether to accept a Monte-Carlo move.

**Parameters**
- score_old : float
  Score before the proposed update.
- score_new : float
  Score after the proposed update.
- kT : float
  Temperature times Boltzmann constant, in pNÅ.

**Returns**
- out : bool
  True for accept, False for reject.

**helixmc.util.read_seq_from_fasta**

helixmc.util.read_seq_from_fasta(fasta)

Read the sequence from a fasta file.

**Parameters**
- fasta : str
  Name of the fasta file.
Returns `seq`: str
Sequence stored in fasta.

Raises ValueError
If the fasta file does not exist.

helixmc.util.locate_data_file

`helixmc.util.locate_data_file(data_file)`
Search for the input data_file. Will look in either current folder or HelixMC data/.

Parameters `data_file`: string
Input numpy array.

Returns `data_file_working`: string
Actual path of the found data file.

Raises ValueError: if the input file does not exist.

### 2.7 Useful Fitting Functions

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>fitfxn.wlc_odijk(F, A, L, S[, kT])</code></td>
<td>Worm-like chain fitting formula described in Odijk 1995 paper.</td>
</tr>
<tr>
<td><code>fitfxn.wlc_bouchiat(A, L, z[, kT])</code></td>
<td>Worm-like chain fitting formula described in Bouchiat et al.</td>
</tr>
<tr>
<td><code>fitfxn.wlc_bouchiat_impl(A, L, S, z, F[, kT])</code></td>
<td>Implicit worm-like chain formula described in Bouchiat et al.</td>
</tr>
<tr>
<td><code>fitfxn.f_wlc_bouchiat_impl(A, L, S, z[, kT])</code></td>
<td>Approximately solve the force from implicit wlc model by grid search.</td>
</tr>
<tr>
<td><code>fitfxn.moroz_3rd(A, C, F[, kT])</code></td>
<td>3rd order Moroz-Nelson function for effective torsional persistence.</td>
</tr>
<tr>
<td><code>fitfxn.moroz_1st(A, C, F[, kT])</code></td>
<td>1st order Moroz-Nelson function for effective torsional persistence.</td>
</tr>
</tbody>
</table>

#### 2.7.1 helixmc.fitfxn.wlc_odijk

`helixmc.fitfxn.wlc_odijk(F, A, L, S[, kT]=41.164043971999995)`
Worm-like chain fitting formula described in Odijk 1995 paper. It is an extensive WLC model.

Parameters `F`: float or 1D ndarray
Z-direction stretching force, in pN.

`A`: float
Bending persistence length, in Å.

`L`: float
Contour length, in Å.

`S`: float
Stretch modulus, in pN.

`kT`: float, optional
Temperature times Boltzmann constant, in pN.Å. Default is 298.15 K.

Returns `z`: float or 1D ndarray
Average Z-extension of the helix, in Å.
Notes

The fitting function \(^1\) is

\[
z = L \left( 1 - \frac{1}{2} \sqrt{\frac{kT}{FA} + \frac{F}{S}} \right)
\]

References

2.7.2 helixmc.fitfxn.wlc_bouchiat

helixmc.fitfxn.wlc_bouchiat \((A, L, z, kT=41.164043971999995)\)

Worm-like chain fitting formula described in Bouchiat et al. 1999 paper. Assumes the chain has constant length (inextensive model). For fitting force-extension curve in low-to-medium force regime (< 10 pN).

Parameters

- \(A\) : float
  Bending persistence length, in Å.

- \(L\) : float
  Contour length, in Å.

- \(z\) : float or 1D ndarray
  Average Z-extension of the helix, in Å.

- \(kT\) : float, optional
  Temperature times Boltzmann constant, in pN.Å. Default is 298.15 K.

Returns

- \(F\) : float or 1D ndarray
  Z-direction stretching force, in pN.

See also:

- wlc_bouchiat_impl Implict worm-like chain fitting formula described in Bouchiat et al.
- f_wlc_bouchiat_impl Approximately solve the force from implicit wlc model by grid search.

Notes

The fitting function \(^1\) is

\[
F = \frac{kT}{A} \left[ \frac{1}{4(1 - z/L)^2} - \frac{1}{4} + \frac{z}{L} + \sum_{i=2}^{i=7} \alpha_i \left( \frac{z}{L} \right)^i \right]
\]

Where \(\alpha = [-0.5164228, -2.737418, 16.07497, -38.87607, 39.49944, -14.17718] \) for \(i = 2\)~7.


References

2.7.3 helixmc.fitfxn.wlc_bouchiat_impl

helixmc.fitfxn.wlc_bouchiat_impl \((A, L, S, z, F, kT=41.164043971999995)\)
Implicit worm-like chain formula described in Bouchiat et al. 1999 paper. Comparison is done in log10(F) space instead (more robust in practice). An extensive rod factor is added for fitting force-extension curve at high-force.

**Parameters**
- **A**: float
  Bending persistence length, in Å.
- **L**: float
  Contour length, in Å.
- **S**: float
  Stretch modulus, in pN.
- **z**: float or 1D ndarray
  Average Z-extension of the helix, in Å.
- **F**: float or 1D ndarray
  Z-direction stretching force, in pN.
- **kT**: float, optional
  Temperature times Boltzmann constant, in pN.Å. Default is 298.15 K.

**Returns**
- **zero**: float or 1D ndarray
  Difference value, should approach zero at perfect fit.

**See also:**
- **wlc_bouchiat** Worm-like chain fitting formula described in Bouchiat et al.
- **f_wlc_bouchiat_impl** Approximately solve the force from implicit wlc model by grid search.

**Notes**

The fitting function (see **wlc_bouchiat** for reference) is

\[
\log_{10} \left[ \frac{kT}{A} \left( \frac{1}{4(1-l)^2} - \frac{1}{4} + l + \sum_{i=2}^{i\leq7} \alpha_i l^i \right) \right] - \log_{10}(F) = 0
\]

With \( l = z/L - F/S \)

2.7.4 helixmc.fitfxn.f_wlc_bouchiat_impl

helixmc.fitfxn.f_wlc_bouchiat_impl \((A, L, S, z, kT=41.164043971999995)\)
Approximately solve the force from implicit wlc model by grid search.

**Parameters**
- **A**: float
  Bending persistence length, in Å.
L : float
Contour length, in Å.

S : float
Stretch modulus, in pN.

z : float or 1D ndarray
Average Z-extension of the helix, in Å.

kT : float, optional
Temperature times Boltzmann constant, in pN.Å. Default is 298.15 K.

Returns F : float or 1D ndarray
Z-direction stretching force, in pN.

See also:

wlc_bouchiat Worm-like chain fitting formula described in Bouchiat et al.
wlc_bouchiat_impl Implicit worm-like chain fitting formula described in Bouchiat et al.

2.7.5 helixmc.fitfxn.moroz_3rd

helixmc.fitfxn.moroz_3rd(A, C, F, kT=41.164043971999995)
3rd order Moroz-Nelson function for effective torsional persistence.

Parameters A : float
Bending persistence length, in Å.

C : float
Torsional persistence length, in Å.

F : float or 1D ndarray
Z-direction stretching force, in pN.

kT : float, optional
Temperature times Boltzmann constant, in pN.Å. Default is 298.15 K.

Returns Ceff : float or 1D ndarray
Effective torsional persistence length in Å. Ceff = L / Var(Lk).

See also:

moroz_1st 1st order Moroz-Nelson function for effective torsional persistence.
The fitting function, originally proposed in reference \(^1\)\(^2\), and summarized in \(^3\), is
\[
C_{\text{eff}} = C \left(1 - \frac{M}{4K_0} + \frac{M^2 - 2M}{16K_0^2} - \frac{4M^3 - 16M^2 + 21M}{256K_0^3}\right)
\]

With
\[
M = \frac{C}{A}, \quad K_0 = \sqrt{\frac{AF}{kT}}
\]

References

2.7.6 \texttt{helixmc.fitfxn.moroz\_1st}

\texttt{helixmc.fitfxn.moroz\_1st} \((A, C, F, kT=41.164043971999995)\)

1st order Moroz-Nelson function for effective torsional persistence. See \texttt{moroz\_3rd} for detailed explanation.

See also:

\texttt{moroz\_3rd} 3rd order Moroz-Nelson function for effective torsional persistence.

Notes

The fitting function is
\[
C_{\text{eff}} = C \left(1 - \frac{M}{4K_0}\right)
\]

With
\[
M = \frac{C}{A}, \quad K_0 = \sqrt{\frac{AF}{kT}}
\]

---


The HelixMC project is authored by Fang-Chieh Chou in 2013, under the supervision of Dr. Rhiju Das, at the Biochemistry Department of Stanford University.

### 3.1 Contacts

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### 3.2 Links

- Source code: https://github.com/fcchou/HelixMC
- HTML documentation: http://helixmc.readthedocs.org/
- Das Lab @ Stanford: http://daslab.stanford.edu

### 3.3 Citing HelixMC

If you use HelixMC in scientific publications, we would appreciate citations to the following paper:


### 3.4 Funding

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